

## EFFECTS OF DOMAIN STRUCTURE ON ELECTRICALLY EXCITABLE MECHANICAL RESONANCES IN FERROELECTRIC CERAMICS

PETER J. CHEN

Sandia National Laboratories, Albuquerque, NM 87185, U.S.A.

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**Abstract**—Recently, I have announced the existence of electrically excitable mechanical resonances in piezoelectric and ferroelectric materials which are not accompanied by any detectable electrical disturbance. These observations are, of course, contrary to conventional understanding, and they are valid for *X*-cut quartz, *Z*-cut LiNbO<sub>3</sub>, slim loop ferroelectrics, PZT65/35, PLZT7/65/35, BaTiO<sub>3</sub> ceramic, Clevite PZT8 and Channel 5500 ceramic, including virgin and thermally depoled specimens of ferroelectric ceramics. In this paper, the effects of domain structure on the existence of the mechanical resonances in the ferroelectric ceramic PZT65/35 are examined. It is shown that domain structure affects not only the number of these resonances but also their amplitudes. These observations are suggestive of the notion that the existence of these mechanical resonances may be due in part to the coupling of the driving electric field to the unit cell dipoles of the domains.

### 1. INTRODUCTION

In two previous papers I have announced the existence of electrically excitable mechanical resonances in piezoelectric and ferroelectric materials which are not accompanied by any detectable electrical disturbance as measured by conventional techniques [1, 2]. These observations are, of course, contrary to conventional understanding. Typically, the onset of a resonance in a piezoelectric or a poled ferroelectric element driven by a cyclic electric field is detected by monitoring the admittance (or impedance) which becomes large (or small) when the resonance occurs. The divergence of the admittance is equivalent to the divergence of the time rate of change of the electric displacement so that the resonance may be viewed as an *electrical* resonance. It is generally believed that the mechanical displacement also diverges during an electrical resonance so that a *mechanical* resonance is said to occur simultaneously.

Experimental determination of the vibrational patterns of resonators is fairly difficult to achieve. Consequently, there are only very limited results in the literature on this subject. In the 1920s and the 1930s there have been some definite attempts to discern the vibrational patterns of quartz crystal resonators, see, e.g. Sections 366–368 of Cady [3]. More recently, Shaw [4], and Shaw and Sujir [5] have examined the vibrational patterns of barium titanate ceramic resonators by employing stroboscopically illuminated multiple beam Fizeau fringes. Of the twelve modes detected in each of the twenty-five cylindrical discs of different diameter to thickness ratios *not a single one* can be identified as the fundamental thickness resonance and *none* approaches uniform piston-like motion as postulated in boundary-initial value problems.† These authors do not allude to the phenomenon described in this paper.

Recently, the mechanical displacements of a piezoelectric or a ferroelectric element driven by a cyclic electric field are monitored using a displacement laser interferometer system. The resolution of the system is well within  $5 \times 10^{-10}$  m (5 Å). With this system mechanical resonances are detected at particular frequencies for many piezoelectric and ferroelectric materials such as *X*-cut quartz, *Z*-cut LiNbO<sub>3</sub>, slim loop ferroelectrics, PZT65/35, PLZT7/65/35, BaTiO<sub>3</sub> ceramic, Clevite PZT8 and Channel 5500 ceramic. Some of the results are reported in the two previous papers [1, 2]. In particular, the mechanical resonant frequencies of two nearly identical thin cylindrical discs of hot-pressed PZT65/35 in the virgin state are given in one of the papers, together with those of one of the discs after thermal annealing at 400°C, and the mechanical and electrical resonant frequencies of the other disc after being poled [1]. In the second paper, the responses of axially poled cylindrical discs of PZT8 ceramic with different diameter to

†In this regard, the reader may also refer to Thurston [6].

thickness ratios are examined [2]. The mechanical resonant frequencies of the discs below the lowest detectable electrical resonances are determined.

In this paper, we examine the effects of domain structure on the existence of the mechanical resonances in the ferroelectric ceramic PZT65/35. It is shown that domain structure affects not only the number of these resonances but also their amplitudes. These observations are suggestive of the fact that the existence of these mechanical resonances may be due in part to the coupling of the driving electric field to the unit cell dipoles of the domains.

## 2. EXPERIMENTAL DETAILS

As we have remarked earlier, the basic instrument which we utilize to determine the mechanical displacements is a displacement laser interferometer system. The essential technical details of the system are given in the paper by Allensworth [7]. In addition, we also determine the electric displacements by monitoring the charge on an integrating capacitor connected in series with the specimens.

The preceding measurements permit the collection of data which are the Lissajous oscilloscope displays of interference fringe intensity versus driving voltage and charge versus driving voltage. These displays not only furnish information regarding the amplitudes of the various quantities but they also exhibit the phase relationships between fringe intensity versus driving voltage and charge versus driving voltage. The phase relationships are crucial in discerning the onset of "resonances". In order to facilitate the ease of data reduction it is helpful though not necessary to limit the amplitude of the driving voltage so that the total change of the interference fringe intensity is less than that of half a fringe. The resolution of the mechanical displacements is such that each centimeter-division on the oscilloscope screen is equivalent to approx.  $5 \times 10^{-10}$  m (5 Å) depending on the intensity of half an interference fringe.

Given the Lissajous displays, it is a simple matter to discern the onset of resonances". In general, at frequencies below that of a resonance the fringe intensity and the charge are in phase with the driving voltage so that the Lissajous displays are straight lines. As the frequency of the driving voltage is increased, say, towards a mechanical resonance the amplitude of the fringe intensity increases together with a phase shift until the fringe intensity and driving voltage are in quadrature, i.e. they are 90° out of phase. At this point the Lissajous display is in the shape of a circle or an ellipse depending on the scales. Continuing increase of the frequency of the driving voltage is accompanied by a decrease of the fringe intensity and further phase shift. Eventually, the fringe intensity and the driving voltage are 180° out of phase so that the Lissajous display is again a straight line but its slope is the negative of what it was originally. Similar observations are valid for the Lissajous display of charge versus driving voltage during the occurrence of an electrical resonance. The preceding observations are consistent with the solution of a second-order ordinary differential equation with a sinusoidal forcing term, and provide us with the opportunity to identify independently the onset of mechanical and electrical resonances. For our present purpose it suffices to regard the frequencies at which fringe intensity versus driving voltage and charge versus driving voltage achieve quadratures as the mechanical and electrical resonant frequencies, respectively.

After attaining the 180° phase shift two things can, in general, happen with regard to a mechanical resonance. First, the amplitude of the fringe intensity may decrease with increasing driving voltage frequency until it vanishes and then reappears so that the fringe intensity and the driving voltage are in phase. This appears as a rotation of the straight line Lissajous display. Second, the fringe intensity and the driving voltage may remain out of phase at 180° with increasing driving voltage frequency until the onset of a succeeding resonance at 90° phase shift. Eventually, the fringe intensity and the driving voltage are again in phase. After an electrical resonance the amplitude of the charge seems to always decrease with increasing driving voltage frequency until it vanishes and then reappears in the in phase condition. These observations suggest that the physical causes of the mechanical resonances may be very complex.

Equivalently, we may also collect the data displayed on a time base. Given the temporal histories of the fringe intensity, the charge and the driving voltage, it is also a simple matter to ascertain the phase relationships between these quantities and the onset of mechanical and electrical resonances. For a particular driving voltage frequency we usually excite only the fundamental of a mechanical resonance unless the amplitude of the driving voltage is very large.

Occasionally, the fundamental and second harmonic are excited. However, the mechanical resonance associated with an electrical resonance exhibits multiple frequencies fairly frequently. In these instances it is possible to excite the fundamental alone if the amplitude of the driving voltage is decreased sufficiently.

The two rectangular specimens which we are examining in the current study are PZT65/35 supplied by Channel Industries, henceforth designated as PZT65/35-C1 and PZT65/35-C2. These specimens are initially in the virgin state. Both specimens have width  $w = 1.524 \times 10^{-2}$  m and length  $l = 5.080 \times 10^{-2}$  m. The thickness of specimen PZT65/35-C1 is  $t = 2.235 \times 10^{-3}$  m, and that of PZT65/35-C2 is  $t = 2.261 \times 10^{-3}$  m.

In order to attain essentially stress-free conditions the specimens are supported on their lower  $w-l$  faces with three ball bearings. The geometry of the spacings of the ball bearings are shown in Fig. 1. The signal beam of the interferometer is directed at the geometric centers of the upper  $w-l$  faces of the specimens at which we have glued very small spectral mirrors. This permits the determination of the mechanical displacements perpendicular to the  $w-l$  plane. However, it is entirely possible that the geometric centers of the  $w-l$  faces of the specimens may be the nodal points of certain resonant vibrational patterns at particular frequencies, and having only small mirrors at the centers need not permit us to determine all the resonant frequencies in some instances. Larger mirrors will undoubtedly affect the responses of the specimens. We are, therefore, exploring the possibility of using highly polished specimens so that the electroded faces are spectral and we may scan these faces.

Specimen PZT65/35-C1 is electroded on its  $w-l$  faces with vapor deposited aluminum of thickness  $3.0 \times 10^{-7}$  m (3000 Å). A sequence of experiments is conducted with this specimen by arranging its domain structure in different configurations. Specimen PZT65/35-C2 is initially electroded on its  $t-l$  faces. After poling the specimen perpendicular to the  $t-l$  plane with a linearly increasing electric field having a maximum magnitude of  $2.1 \times 10^6$  V/m at 25 s (remanent polarization being  $0.3657$  C/m<sup>2</sup>), the specimen is returned to an electrically neutral state exhibiting no remanent polarization by slowly varying the switching field. In this state there are more dipoles essentially parallel to the  $w-l$  plane than the other two planes. The electrodes on the  $t-l$  faces are then removed and the  $w-l$  faces are electroded with vapor deposited aluminum of thickness  $3.0 \times 10^{-7}$  m (3000 Å).

Another specimen which we are examining is a piece of initially virgin hot-pressed PZT65/35 in the shape of a cylindrical disc prepared at our Laboratories, henceforth designated as PZT65/35-S2. It has a diameter of  $3.607 \times 10^{-2}$  m and a thickness of  $8.128 \times 10^{-4}$  m. The center circular region of the faces of the disc with diameter  $1.793 \times 10^{-2}$  m are electroded with vapor deposited aluminum of thickness  $3.1 \times 10^{-7}$  m (3100 Å). The disc is symmetrically supported on three ball bearings equally spaced at  $1.270 \times 10^{-2}$  m. Here, it is held in contact with the ball bearings by three small springs directly over the locations of the ball bearings and exerting a total force of less than  $6.675 \times 10^{-2}$  N. A very small spectral mirror is glued at the center of the top face. The axial mechanical displacements of the disc are determined using the laser interferometer system.

### 3. EXPERIMENTAL RESULTS

Temperature fluctuations and residues of fluids used to clean the specimens affect not only the resonant frequencies but also the magnitudes of the mechanical displacements as deter-

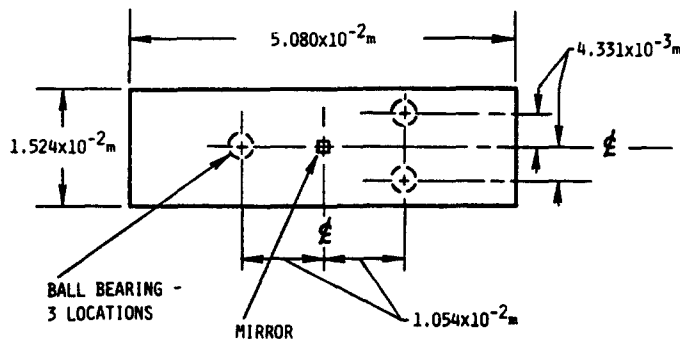


Fig. 1. Geometry of support conditions of specimens PZT65/35-C1 and PZT65/35-C2.

mined by the laser interferometer. Accordingly, the specimens are usually allowed to stabilize for at least 12 hr after being placed in their test configurations, and the entire system including the laser interferometer is enclosed. The temperature within the enclosure is maintained at a constant 25.6°C. This procedure ensures that the results obtained are as repeatable as possible. The magnitudes of the mechanical displacements and to a much lesser degree the resonant frequencies may also be affected by the spacings of the support ball bearings. The reason for this is quite obvious because the measured values of the mechanical displacements depend on the vibrational patterns whose manifestations in turn depend on the support conditions. It is, nevertheless, meaningful and useful to compare results between different specimens for the same support conditions and between different resonant frequencies for the same specimen.

We have also noticed that the resonant frequencies and the peak mechanical displacements of the mechanical resonances are quite repeatable before the specimens are allowed to resonate electrically. Immediately after a specimen has resonated electrically there are appreciable changes in the frequencies and displacements of its mechanical resonances. However, if the specimen is allowed to stabilize for sufficiently long time, e.g. 12 hr, its former results are again obtained. The reasons for this are not understood at this time—one reason may be that the specimen is heated due to power dissipation during an electrical resonance.

The results reported in this paper are taken after the specimens have been allowed to stabilize. However, in instances for which we give the mechanical resonances between electrical resonances the data are taken sequentially with increasing driving voltage frequencies. This is because it is not convenient to allow the specimens to stabilize in order to determine the characteristics of the mechanical resonances which occur between electrical resonances.

As we have remarked earlier the domain structure of specimen PZT65/35-C1 is arranged in various different configurations and a sequence of experiments is conducted during the process. From the virgin state, the specimen is subjected to three and a half cycles of a linearly varying cyclic electric field with amplitude  $1.566 \times 10^6$  V/m and period 100 s. The corresponding remanent polarization is  $+0.3617$  C/m<sup>2</sup>. The electrically neutral state is then established by slowly varying the switching field. However, we did not attain true electrical neutrality in this instance and the residual polarization is  $-6.5 \times 10^{-3}$  C/m<sup>2</sup> which is about 1.8% of the remanent polarization. From this electrically neutral state the specimen is thermally annealed at 400°C for 1 hr. By poling the specimen with a linearly increasing electric field having a maximum magnitude of  $1.566 \times 10^6$  V/m in 25 s, a remanent polarization of  $+0.2777$  C/m<sup>2</sup> is attained indicative of the fact that the switching characteristics of the domains have altered. Again, the specimen is annealed at 400°C for 1 hr and poled with a linearly increasing electric field having a maximum magnitude of  $1.544 \times 10^6$  V/m in 25 s. This time the remanent polarization is  $0.3061$  C/m<sup>2</sup>. Notice that besides the virgin state and the electrically neutral state, we have two thermally depoled states and three poled states. No mechanical resonances are detected for this specimen in the virgin state at the geometric center of its upper  $w-l$  face. In Tables 1 and 2, we compare the results for the two thermally depoled states and the three poled states, respectively. The results corresponding to the electrically neutral state are compared to those corresponding to the laterally electrically neutral state of specimen PZT65/35-C2 in Table 3.

Specimen PZT65/35-S2 is first poled with a linearly increasing electric field with maximum magnitude  $2.1 \times 10^6$  V/m in 25 s (remanent polarization being  $0.3365$  C/m<sup>2</sup>), arranged in the electrically neutral state, and poled again with the same electric field. Since the results corresponding to the virgin state and the first poled state are reported in a previous paper[1], they will not be repeated here. Hence, we shall record the results corresponding to the electrically neutral state and the second poled state, and they are given in Table 4.

#### 4. DISCUSSIONS

Table 1 shows that the frequencies of the mechanical resonances exhibited by the specimen PZT65/35-C1 in the two thermally depoled states are quite consistent while the peak mechanical displacements of the resonances associated with the first thermally depoled state are generally larger than those associated with the second thermally depoled state. We know that the domain structures of the two states are different because their domain switching characteristics from

Table 1. Mechanical resonant frequencies and peak mechanical displacements of thermally depoled PZT65/35-C1

PZT65/35-C1			
First Thermally Depoled State		Second Thermally Depoled State	
Resonant Frequencies	Peak Mech. Displ.	Resonant Frequencies	Peak Mech. Displ.
1.372 kHz	$2.0 \times 10^{-10} \text{m}$	1.468 kHz	$0.6 \times 10^{-10} \text{m}$
1.969 kHz	$1.11 \times 10^{-9} \text{m}$	2.010 kHz	$0.6 \times 10^{-10} \text{m}$
3.429 kHz	$4.59 \times 10^{-9} \text{m}$	3.464 kHz	$0.6 \times 10^{-10} \text{m}$
17.049 kHz	$6.3 \times 10^{-10} \text{m}$	17.050 kHz	$1.7 \times 10^{-10} \text{m}$
35.110 kHz	$4.7 \times 10^{-10} \text{m}$	35.239 kHz	$0.3 \times 10^{-10} \text{m}$
40.110 kHz	$6.7 \times 10^{-10} \text{m}$	40.184 kHz	$1.7 \times 10^{-10} \text{m}$
43.072 kHz	$1.5 \times 10^{-10} \text{m}$		
59.470 kHz	$0.5 \times 10^{-10} \text{m}$	59.619 kHz	$0.6 \times 10^{-10} \text{m}$
71.448 kHz	$0.5 \times 10^{-10} \text{m}$	71.422 kHz	(No data taken)
83.166 kHz	$0.5 \times 10^{-10} \text{m}$	83.068 kHz	(No data taken)
107.168 kHz	$0.5 \times 10^{-10} \text{m}$	(No additional	
123.811 kHz	$0.5 \times 10^{-10} \text{m}$	data taken)	

Amplitude of driving voltage: 5V RMS.

Table 2. Resonant frequencies and peak mechanical displacements of poled PZT65/35-C1

PZT65/35-C1					
First Poled State, ( $0.3617 \text{ C/m}^2$ )		Second Poled State <sup>1</sup> , ( $0.2777 \text{ C/m}^2$ )		Third Poled State <sup>2</sup> ( $0.3061 \text{ C/m}^2$ )	
Resonant Frequencies	Peak Mech. Displacements	Resonant Frequencies	Peak Mech. Displacements	Resonant Frequencies	Peak Mech. Displacements
2.000 kHz	$8.37 \times 10^{-9} \text{m}$	2.017 kHz	$7.35 \times 10^{-9} \text{m}$	2.111 kHz	$6.49 \times 10^{-9} \text{m}$
3.555 kHz	$9.16 \times 10^{-9} \text{m}$	3.487 kHz	$1.53 \times 10^{-8} \text{m}$	3.529 kHz	$2.03 \times 10^{-8} \text{m}$
17.566 kHz	$9.6 \times 10^{-10} \text{m}$	17.330 kHz	$1.84 \times 10^{-9} \text{m}$	17.350 kHz	$1.01 \times 10^{-9} \text{m}$
E35.782 kHz <sup>3</sup>		E35.724 kHz <sup>3</sup>		E35.673 kHz <sup>3</sup>	
41.425 kHz	$2.55 \times 10^{-9} \text{m}$	40.709 kHz	$1.99 \times 10^{-9} \text{m}$	40.995 kHz	$1.26 \times 10^{-9} \text{m}$
		43.973 kHz	$9.4 \times 10^{-10} \text{m}$	44.246 kHz	$8.0 \times 10^{-10} \text{m}$
E123.319 kHz	$9.65 \times 10^{-9} \text{m}$	E123.584 kHz	$7.68 \times 10^{-9} \text{m}$	E123.325 kHz	$7.40 \times 10^{-9} \text{m}$

Amplitude of driving voltage: 5V RMS.

Electrical resonances are prefixed by the letter E.

<sup>1</sup>Phase shift between fringe intensity and driving voltage detected at 1.393 kHz.

<sup>2</sup>Phase shift between fringe intensity and driving voltage detected at 1.645 kHz.

<sup>3</sup>Associated mechanical resonances exhibit multiple frequencies.

Table 3. Resonant frequencies and peak mechanical displacements of electrically neutral PZT65/35-C1 and laterally electrically neutral RZT65/35-C2

PZT65/35-C1 Electrically Neutral State <sup>1</sup>		PZT65/35-C2 Laterally Electrically Neutral State	
Resonant Frequencies	Peak Mech. Displ.	Resonant Frequencies	Peak Mech. Displ.
1.339 kHz	$4.7 \times 10^{-10} \text{m}$	1.437 kHz	$4.1 \times 10^{-10} \text{m}$
1.854 kHz	$1.43 \times 10^{-9} \text{m}$	1.979 kHz	$2.6 \times 10^{-10} \text{m}$
3.458 kHz	$1.07 \times 10^{-8} \text{m}$	3.559 kHz	$3.3 \times 10^{-10} \text{m}$
		6.415 kHz <sup>2</sup>	
		9.437 kHz	$5.0 \times 10^{-10} \text{m}$
		13.112 kHz	$9.6 \times 10^{-10} \text{m}$
17.394 kHz	$3.66 \times 10^{-9} \text{m}$	17.576 kHz	$2.52 \times 10^{-9} \text{m}$
		20.508 kHz <sup>3</sup>	
		28.413 kHz	$3.7 \times 10^{-10} \text{m}$
		30.242 kHz <sup>4</sup>	$3.7 \times 10^{-10} \text{m}$
35.842 kHz	$5.4 \times 10^{-10} \text{m}$	34.689 kHz	$9.2 \times 10^{-10} \text{m}$
41.201 kHz	$6.9 \times 10^{-10} \text{m}$	40.614 kHz	$7.78 \times 10^{-9} \text{m}$
		59.901 kHz	$3.59 \times 10^{-9} \text{m}$
		71.339 kHz	$5.5 \times 10^{-10} \text{m}$
		73.437 kHz	$3.8 \times 10^{-10} \text{m}$
		84.118 kHz	$2.30 \times 10^{-9} \text{m}$
		97.933 kHz	$5.0 \times 10^{-10} \text{m}$
		112.989 kHz	$1.43 \times 10^{-9} \text{m}$
125.615 kHz	$6.5 \times 10^{-10} \text{m}$	128.339 kHz	$3.5 \times 10^{-10} \text{m}$

Amplitude of driving voltage: 5V RMS.

<sup>1</sup>Phase shifts between charge and driving voltage detected at 17.866 kHz, 59.544 kHz and 90.040 kHz. Phase shift between fringe intensity and driving voltage detected at 1.382 kHz.

<sup>2</sup>Excitation of the second harmonic.

<sup>3</sup>Resonance exhibits multiple frequencies.

<sup>4</sup>Accompanied by phase shift between charge and driving voltage.

these states are different yielding different states of remanent polarization for essentially the same applied electric field.

The mechanical and electrical resonant frequencies exhibited by the specimen PZT65/35-C1 (Table 2) in the three poled states are again quite consistent even though they have different remanent polarizations. There does not seem to be any correlation between the values of the remanent polarizations and the peak mechanical displacements. Notice that electrical resonances now occur at 35 kHz and 123 kHz which show up as mechanical resonances in the thermally depoled states.

All the mechanical resonant frequencies exhibited by the specimen in the thermally depoled states also occur as mechanical or electrical resonant frequencies in the poled states except at 59, 71, 83 and 107 kHz. Similar mechanical resonances at 59, 71, 84 and 112 kHz and others also occur in specimen PZT65/35-C2 whose domains are arranged in the laterally electrically neutral state, but not in specimen PZT65/35-C1 when its domains are arranged in the electrically neutral

Table 4. Resonant frequencies and peak mechanical displacements of electrically neutral and poled PZT65/35-S2

PZT65/35-S2 Electrically Neutral State <sup>1</sup>		PZT65/35-S2 Second Poled State <sup>2</sup>	
Resonant Frequencies	Peak Mech. Displ.	Resonant Frequencies	Peak Mech. Displ.
2.179 kHz	$8.6 \times 10^{-10} \text{m}$	1.493 kHz	$8.6 \times 10^{-10} \text{m}$
5.458 kHz	$9.27 \times 10^{-9} \text{m}$	2.173 kHz	$7.85 \times 10^{-9} \text{m}$
6.181 kHz	$5.96 \times 10^{-9} \text{m}$	2.607 kHz <sup>3</sup>	
17.592 kHz	$1.09 \times 10^{-8} \text{m}$	5.439 kHz	$1.41 \times 10^{-8} \text{m}$
		5.838 kHz	$1.6 \times 10^{-10} \text{m}$
		6.103 kHz	$4.19 \times 10^{-9} \text{m}$
		17.301 kHz } <sup>4</sup>	$3.9 \times 10^{-10} \text{m}$
		17.953 kHz }	$2.52 \times 10^{-9} \text{m}$
		27.747 kHz }	$1.03 \times 10^{-9} \text{m}$
		41.037 kHz	$1.86 \times 10^{-9} \text{m}$
68.833 kHz	$6.4 \times 10^{-10} \text{m}$	69.928 kHz	$2.10 \times 10^{-8} \text{m}$
105.042 kHz	$4.6 \times 10^{-10} \text{m}$	72.078 kHz	$5.82 \times 10^{-9} \text{m}$
146.676 kHz	$4.0 \times 10^{-10} \text{m}$	148.839 kHz	$4.3 \times 10^{-10} \text{m}$
		187.492 kHz	$2.54 \times 10^{-9} \text{m}$
190.316 kHz	$1.51 \times 10^{-9} \text{m}$	189.561 kHz	$8.01 \times 10^{-9} \text{m}$
		194.138 kHz	$2.52 \times 10^{-9} \text{m}$

Amplitude of driving voltage: 5V RMS.

Electrical resonances are prefixed by the letter E.

<sup>1</sup>Phase shifts between fringe intensity and driving voltage detected at 1.397 kHz, 124.853 kHz. Possible mechanical resonances at 28.281 kHz, 39.234 kHz and 39.867 kHz - barely detectable.

<sup>2</sup>Phase shifts between fringe intensity and driving voltage detected at 1.354 kHz, 9.826 kHz and 53.655 kHz.

<sup>3</sup>Mechanical resonance consists of the fundamental and the second harmonic.

<sup>4</sup>Fringe intensity and driving voltage achieve quadrature successively without achieving 180° phase shift between these frequencies.

state (Table 3). In the laterally electrically neutral state there are more dipoles essentially parallel to the  $w-l$  plane (perpendicular to the driving field) than the other two planes. This is suggestive of the notion that these mechanical resonances can be due to the coupling of the driving voltage to the perpendicular dipoles. This observation is substantiated by two facts. First, in the electrically neutral state, there are more dipoles parallel to the driving field than the other two directions and these mechanical resonances are not detected. Second, the peak mechanical displacements associated with these mechanical resonances are much larger than those in the thermally depoled states.

The mechanical resonant frequencies of specimen PZT 65/35-C1 in the electrically neutral state are consistent with the mechanical and electrical resonant frequencies of specimen PZT65/35-C1 in the poled states. In these instances there are more dipoles parallel to the driving field than the other two directions, and these resonances can be due to the coupling of the driving voltage to the parallel dipoles which may be easier to excite. Notice that the peak mechanical displacement of the mechanical resonance at 3.4-3.5 kHz remains large, independent of whether specimen PZT65/35-C1 is poled or is in the electrically neutral state.

The mechanical and electrical resonant frequencies of specimen PZT65/35-S2 in the second poled state (Table 4) are consistent with those reported in a previous paper for the first poled state[1]. The domain structures of the two states are, of course, different. Therefore, differences in the peak mechanical displacements are detected, but they are of comparable magnitudes. The interesting results of the specimen PZT65/35-S2 occur in the electrically

neutral state. First, a mechanical resonance is detected at 190 kHz which shows up as an electrical resonance at 189 kHz in the second poled state, but nothing analogous occurs at 72 kHz. Second, the peak mechanical displacement of the mechanical resonance at 17 kHz is quite large when specimen PZT65/35-S2 is in the electrically neutral state. Curiously, the same is true for the 17 kHz mechanical resonance of specimens PZT65/35-C1 and PZT65/35-C2 in either of the electrically neutral states.

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